HYDRAULIC MODEL STUDIES OF MECHANICAL MIXING DEVICES IN STRATIFIED LAKES

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ABSTRACT

The investigation was undertaken to analyze the effectiveness of devices for artificially destratifying lakes. A criterion for the effectiveness of mixing was selected. This criterion was applied to a number of variations of mechanical mixing devices in an attempt to indicate trends in optimization of designs. Experiments were performed in a vertically exaggerated scale model of Ham's Lake. Destratification was accomplished by a jet of water from two different sizes of propellers in different configurations (shrouded, skirted, and free) mixing the top water with the bottom water. Data taken from the experiments included density profiles as a function of time. The data obtained were analyzed determining the progression of the stability index with time.

Adequate simulation of the prototype destratification experiments of Steichen (10) was achieved with the present model. The appropriate non-dimensional parameters are the overall Richardson number $J = g\Delta\rho H/\rho U^2$, and a characteristic time obtained from the volume of the lake divided by the volume flow rate of the pump. Analyzing the effects of varying propeller size and geometrical constraints on mixing efficiency revealed the following facts: Operation of a pump with a shrouded propeller resulted in a shorter destratification time and higher destratification efficiency than an unshrouded propeller when both pumps had the same power consumption rates. For the pump system operating with an unshrouded propeller increasing propeller size resulted in increased destratification efficiency over the shaft input power range studies.

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NOMENCLATURE

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DE

Fr

h

destratification efficiency =

net change in stability from t_1 to t_2 total energy input from t_1 to t_2 × 100

g gravitational constant

height of center of gravity of the lake/model from the bottom

H maximum depth of lake or basin

J basic definition of overall Richardson number = $\frac{g\Delta\rho L}{\rho U^2}$

L a characteristic length

Q volume flow rate of pump

Re Reynolds number =
$$\frac{UL}{v}$$

Ri Richardson number =
$$\frac{-g_{\partial \rho}/\partial z}{\rho(\partial u/\partial z)^2}$$

SI nondimensional stability index = $\frac{\rho g(h_h - h)}{\rho g(h_h - h_s)}$

t time

u

te characteristic time of mechanical destratification = $\frac{V}{Q}$

t* nondimensional time = $\frac{t}{t_c}$

local velocity in the X direction

- U characteristic velocity
- V volume of lake or model basin

Greek Letters

- ν kinematic viscosity
 ρ fluid density
- P_t initial density at surface of water

Subscripts

d destratification h homogeneous m model p prototype s stratified

CHAPTER I

INTRODUCTION

Thermal stratification occurs in almost all lakes and reservoirs. In shallow impoundments the stratification may be weak. In deep lakes and reservoirs in which the storage volume is large compared to the annual throughflow, strong stratification is generally developed. The hydraulic model developed in this study is concerned with the latter situations in which the water temperature is a function of depth and time.

According to a study by Harleman et al. (1):

The primary causes of thermal stratification are the low thermal conductivity of water, the limited penetration of radiant heat and light, and the fact that stream inflows tend to be warmer than reservoir surface water. Usually all heat, apart from advected heat enters the reservoir through the surface in the form of the radiant energy. A high percentage of this energy is absorbed in the top few meters and thus the water near the surface is heated more quickly than the lower layers. This warm water tends to stay at the surface, absorbs more heat, and produces a stable condition. However, evaporation will always cool the surface causing convection currents. Surface cooling and convection will be enhanced by back radiation and conduction losses, especially at nights. Wind stresses on the water surface will cause mixing whenever neutral or unstable density gradient is set up by surface cooling. These processes of heating, cooling, and wind action lead to the development of a warm, freely circulating, turbulent upper region, called the epilimnion (p. 1).

It shields a colder, denser, relatively undisturbed region called the hypolimnion. The stratum of rapid temperature change is known as the thermocline. When these conditions exist, the reservoir is said to be stratified. Under thermally stratified conditions, with circulation to

the hypolimnion impeded by the thermocline, renewal of oxygen from the atmosphere cannot take place in the lower layers. This can lead to an anaerobic state and poor water quality. During a later overturn, the mixing of these waters with the rest of the reservoir may pollute all the water for a short period. Furthermore, release of this poor quality water may cause a deterioration of water quality downstream of the impoundment.

Field Research

Three types of attempts have been made to artificially mix densitystratified impoundments.

1. Mixing caused by releasing compressed air bubbles at depth.

2. Mixing caused by the discharge of a jet of water into the impoundment.

3. Mixing caused by the use of a submerged pumping system. Symons et al. (2, 3) forced compressed air from diffuser stones at the bottom of the impoundment to create air-bubble plumes which induced mixing. Successful elimination of the stratification, and water quality improvement in reservoirs are reported by Knoppert et al. (4), Symons et al. (5), and Lackey (6). An attempt to find an optimum mechanical aeration system was reported by Hogan et al. (7).

The second type of technique used in attempting to mix stratified impoundments is that of the mechanical pumping system with assorted piping. It consists of pumping apparatus which simply takes water from one elevation in the impoundment and jets it out at another. Irwin et al. (8) used this technique to pump cold dense water from near the bottom to the surface of the lake.

The third type of technique was investigated by Quintero and Garton (9) and Steichen (10) using submerged axial-flow pump to move the oxygen-rich water from the surface of a lake to the oxygen-deficient water at the bottom. The application of mechanical pumping systems for mixing impoundments has been more limited than the use of compressed air systems. However, pumping systems have shown successful results in mixing process and may be designed to operate more efficiently than air systems.

Significance of Modeling

Although destratification devices of moderate size have been built by others, it has not been economically possible to try out different configurations or to optimize the design. The design parameters have largely been selected on the basis of intuition and availability. The possibility of a different more effective configuration is unknown. A large portion of the energy input is wasted and only a small percentage goes into actual mixing of fluids from different strata. In order to minimize the energy loss and the size and cost of these devices, it is important to raise the effectiveness of these components, especially if larger reservoirs are to be mixed. Since one stratification experiment on a prototype lake takes at least one summer, the advantages of a laboratory model, with the capability to run several experiments in a much shorter time are obvious. The obtained results will aid in the optimal design of destratification devices and in the sizing and selection of units for particular applications.

Background in Lake Modeling

There has been considerable amount of work done in the past few years pertinent to the topics of lake destratification and to modeling of various lake flow situations. Several mathematical models have been developed to analyze the flow situations in lakes and reservoirs. Mathematical models based upon the one-dimensional heat transfer equation for heat flux, absorption and transmission of solar radiation, and properties of circulation in stratified lakes have been developed by Dake and Harleman (11), Ryan and Harleman (1), and Lugget and Lee (12). Simulation models have also been developed to analyze the applicability of these techniques to lakes and reservoirs. An example of which is a model generated by Ditmar (13) for the prediction of changes in the density structure of an impoundment due to mixing by a pumping system.

There is active research in the general area of hydraulic modeling, some involving stratified bodies of water. One example is modeling the hydraulics and thermal dispersion in an irregular estuary by Boericke and Hall (14). An interesting example of work done on hydraulic models is the design of a new type of water channel with density stratification by Odell and Kovaszny (15).

Of particular importance of the present study is the ongoing research of Quintero and Garton (9) which involves the full scale testing of particular destratification device. Quintero and Garton (9) have reported the temperature and dissolved oxygen distributions in Ham's lake which they mechanically destratify with a large pump. The destratification experiment which is modeled in the present study is the situation in which the prototype lake is initially strongly stratified.

(This is primarily a seasonal thermal stratification.) The experiment begins with turning on of the mechanical pump which destratifies the prototype lake in from one to three weeks. This experiment is the experiment of most importance in meeting the objectives of the present study, to develop the modeling technique in stratified lake flows to the state where reliable prediction of prototype lake mixing phenomenon is possible. The model is Ham's lake constructed by Gibson (16) was the basic facility used in the present study. The major features of present model experiments are:

1. The lake is initially strongly stratified.

2. The destratification pump is a model of the one used by Steichen (10).

3. The lake model has vertical scale exaggeration.

The density differences in the prototype lake may be due to temperature differences; in the model, thermal stratification is impractical. The required temperature differences are too great, the boundary conditions of conduction from the bottom of the lake or radiation, convection, and mass transfer from the surface are not the same in the model and the prototype. However, if the fluid has similar thermal and molecular diffusivity (i.e., if the Lewis number is near 1) or if the major mechanism of mixing is turbulent rather than diffusion--both of which conditions are true in this case--density differences due to temperature may be modeled by density differences due to dissolved salts.

There are a number of salts which can increase the density of water by about 80%; common table salt can give about a 20% increase--less if the solution has to be clear--but it is convenient and inexpensive and a

few percent weight density increase is adequate for the needed experiments.

Although there is considerable experience in the literature with modeling with vertical scale exaggeration (17, 18, 19) and with stratified water ways (20), no report was found of hydraulic model studies which involve all three of the major features of present model experiment listed above. The distorted model used with the present study has a horizontal scale factor of 1 to 360 and vertical scale factor of 1 to 34. The practice of scale distortion can be subjected to much criticism. Fisher and Holley (17) have stated that distorted models should not be used to model dispersion since "a distorted hydraulic model magnifies the dispersive effects of vertical velocity gradients and diminishes the effects of transverse gradients" (p. 51). However, Keulegan (21) and Barr and Hassan (22) have reported moderately good success in modeling exchange flows in rectangular channels with distorted hydraulic models. One of the major questions of interest in the present study is what experimental data could be obtained, in direct or corrected form, which will be useful for the predictive purposes.

Objective

The major goal of the present study was to determine the relative mixing efficiencies of different pump configurations. The major objectives of the study can be broken down into three categories.

1. To determine the effect of varying propeller size on mixing efficiency.

2. To determine the effects of geometrical constraints on mixing efficiency. (I.e., does a jet with a shroud or diffuser have a higher

mixing efficiency than a free jet?)

3. To determine if results obtained from model experiments can be justifiably applied to the prototype situation.

CHAPTER II

IMPORTANT DEFINITIONS AND PARAMETERS

This chapter is intended to present the modeling parameters, such as scale factors, related nondimensional numbers, and in particular Richardson Number. The important definitions, such as stability index and destratification efficiency used throughout this text, are also presented in this chapter and their significance is discussed in detail.

Modeling Parameters

In modeling any free surface stratified hydraulic system, three nondimensional parameters are of importance. These three parameters are:

1. Froude Number:

$$Fr = \frac{U}{(gL)^{1/2}};$$

2. Reynolds Number:

Re =
$$\frac{UL}{v}$$
;

3. Richardson Number:

$$Ri = \frac{-g\partial\rho/\partial z}{\rho(\frac{\partial u}{\partial z})}.$$

Froude number becomes a part of the governing equation if there is an open surface, as on a lake, with a high density below it and a negligible density above it. In flow situations such as one being analyzed

in the present study, where the open surface waves are negligible and the entire surface of the lake is assumed to be at the same level, Froude number becomes an unimportant parameter. Such would not be the case if there were substantial mean current due to a throughflow in the lake. However, in the model the Froude number is large; it may, for example, reach a critical value at which the surface depression over pump inlet may be so great that air is entrained and cavitation occurs. It is necessary to limit the velocity increase and size reduction in the model to make sure that the Froude number does not become important.

The consequence of limiting Froude number is that either the models must be large (i.e., the characteristic length reduced by only a moderate ratio, and the reference velocity increased by only the same ratio); or that the Reynolds number is lower in the model than in the prototype (i.e., the reference velocity is not increased in proportion to the scaling ratio). There is considerable experience in the use of toosmall Reynolds numbers in models. It is known that this deviation from strict similitude leads to only moderate errors, if the flow regimes (i.e., laminar or turbulent Flow) are still the same in the model. The situation will be discussed later where there is less mixing in the model, due to the lower Reynolds number (Chapter IV).

Another possible compromise is the use of geometric distortions. For example, the horizontal scale may be chosen to be a very small ratio (1 to 360 in this case), so that the model will fit into a given facility, while the vertical scale is a bigger ratio (i.e., 1:34 in this case), so that lower Froude numbers and higher Reynolds numbers (for the boundary layer on the bottom) are possible. However, this represents a deviation from the prototype as mentioned by Fisher and Holley (17)

which cannot be analyzed in terms of similitude. As one objective of this study, experiments were attempted to examine this problem in some detail.

Richardson number is the most important nondimensional parameter in hydraulic modeling of stratified flows. This parameter relates to the terms of the governing equation which are most important to the phenomena concerned with the primary objective of this study. In the form of densimetric Froude number or its inverse, overall Richardson number is defined to be

$$J = \frac{g\Delta\rho L}{\rho U^2}$$

where $\Delta \rho$ is a reference density difference (i.e., difference in the density between the top and bottom of the lake) and L is the characteristic length, taken vertically if there is a geometric distortion. Overall Richardson number is derived from the gradient Richardson number

$$R_{i} = \frac{-g\partial\rho/\partial z}{\rho(\frac{\partial u}{\partial z})}$$

by assuming that the density gradient $\frac{\partial \rho}{\partial z}$ scales with a characteristic density difference $-\Delta \rho$ divided by a characteristic length, L, and the velocity gradient scales with a characteristic velocity U divided by L. To match Richardson number between model and prototype, where the depth of the model is smaller but its reference velocity greater than in the prototype, the density difference in the model must be greater in order to achieve the same Richardson number.

It is important to realize that even though the model is geometrically distorted, the mixing process is undistorted. This is a resulting fact from scaling the propeller 1:34 like vertical scale, so that the

near field modeling would be undistorted. However, the supply of unmixed fluid available to the process is reduced beyond 1:34. For the purpose of obtaining time scales of mixing the overall lake, the volume of the lake divided by the volume flow rate of the propeller was chosen as a characteristic time. This relates the mixing rate to the total basin to be mixed. Observing the dispersion of dye from above and through the dam (16), bore out the following fact: the mixing took place largely in the vicinity of the destratification propeller and the mixed, intermediate density liquid flowed outward at its proper level as a "lens." From this the important assumption was developed that the limiting process is the mixing phenomenon in the zone which was modeled correctly, and that the transport phenomenon is not the limiting factor. The time in which the mixed fluid reaches the farthest part of the lake is short (and should remain short even without geometric distortion) compared to the time necessary for total mixing. Hence we condlude that the approach used in the present study, which concentrates on the mixing process and neglects the dispersion time, is appropriate for predicting the progress of destratification as an overall process.

Criterion for Evaluating Destratification

The stability of the stratification is an important phenomenon since it quantifies the amount of energy necessary to overcome an existing stratification condition. In nondimensional form the stability index is

$$SI = \frac{\rho g(h_h - h)}{\rho g(h_h - h_s)}$$

where h is the height from the bottom of the center of gravity of the

lake, ρ is the average lake density, and the subscripts h and s stand for homogeneous and fully stratified, respectively. The stability index is the gravitational potential energy of the lake referenced to the lake in its homogeneous condition and nondimensionalized with the potential energy of the fully stratified lake (with the same reference). This index is computed from the density profiles and the elevation contours of the lake which provided the volume of the lake in every increment of elevation. If profiles are taken over a period of time calculations can be made to generate stability index versus time curves. A criterion was chosen that the model was destratified when the stability index fell below 10% of its initial value. Corresponding time for this value of stability index was called t_d^* (nondimensional destratification time).

Destratification Efficiency

Calculation and comparison of the "destratification efficiency" is a useful way of comparing the mechanical performance of artificial destratification devices. A means of calculating the effectiveness of a destratification apparatus is suggested by Symons et al. (3) in the form of the destratification efficiency (DE), defined by the ratio:

 $DE = \frac{\text{Net change of stability from } t_1 \text{ to } t_2}{\text{Total energy input from } t_1 \text{ to } t_2} \times 100.$

It is difficult to determine in generalized terms the input energy required to drive a particular pumping system. A major portion of the losses in a system are unique to the particular pumping system and its detailed design. While consideration of these details is important to the design of a particular pumping system, the purpose of this study is

to find results which will guide the general, rather than detailed, design of the system.

CHAPTER III

PROTOTYPE DESTRATIFICATION

Ham's lake, 8 kilometers west of Stillwater, was chosen as the lake to be modeled. Ham's lake was built by the Soil Conservation Service of the United States Department of Agriculture in 1964. The surface area of the lake is 40 hectars and it has a volume of 115 hectar-meters. The lake has a maximum depth of approximately 9 meters near the dam. Figure 1 shows a map of Ham's lake. Garton and his students (e.g., Steichen [10]) have continued to conduct destratification experiments each year on Ham's lake as well as on larger lakes. The researchers used a large propeller connected to a one-half horsepower motor to force the top water downward. The propeller was enclosed in a cylindrical housing and the velocity of the water leaving the propeller was measured by a screwtype current meter located beneath the propeller. Details of pumping device used to destratify this lake and its performance are described by Quintero and Garton (9). A sketch of the pumping device used is shown in Figure 2. The researchers continuously recorded the temperature and dissolved oxygen profiles at different locations during the destratification process. Toetz, Wilhm and Summerfelt (23) have analyzed the general aspects of the biological effects of artificial destratification in Ham's lake. They have continued to monitor important biological information, including fish growth, on the lakes Garton (9) has been destratifying.

On July 16, 1973, Steichen (10) began continuous operation of the destratification pump (without the conical skirt) in Ham's lake. He reported that during the mechanical destratification of a lake, temperature (and hence density) profiles taken at different locations in the lake are not substantially different. Figure 3 is a reproduction of the average temperature profile he measured on that day and density profile deduced from the temperatures. Table I lists the pertinent information about the lake and the pump for this operation. Based upon the initial density difference and using the pump average outlet velocity as the characteristic velocity, the Richardson number for this flow calculates to be $J = \frac{q(\Delta \rho / \rho)H}{U^2} = .398$. The pertinent fluid dynamic data from this experiment can be summarized in Figures 4 and 5. Figure 4 shows a record of the density profiles measured (from temperature readings) throughout the prototype destratification experiment.

Conventional analysis of this type of data includes a calculation of the progress of the stability index with time. The progress of the stability index with time during the prototype destratification experiment is plotted in Figure 5. The time variable t has been nondimensionalized with the characteristic time t_c for this phenomenon defined as the ratio of the total volume of the lake divided by the volume flow rate of the pump, i.e., $t_c = \frac{V}{Q}$ and $t^* = \frac{t}{t_c}$. A fourth order polynomial least squares regression curve fit has been made to this data and yields the curve in the figure. The portion of the curve from the prototype experiment which shows a stability index increase between the nondimensional times of 1.2 and 1.5 is due to the climatological effects. This type of effect was not modeled in the present research program. Using the 10% stability index criterion, the value of $t_d^* = .76$ ($t_d = 15.1$ days) is obtained for the prototype experiment. This nondimensional destratification time is one of the most important parameters of the physical process which is hoped to be able to predict with the use of the hydraulic model in the present study.

CHAPTER IV

EXPERIMENTAL APPARATUS

In this chapter the experimental apparatus and procedures are described. The test facilities are essentially those used by Gibson (16) with some additions and modifications.

Model Basin

A 3785 liters basin with the model of Ham's lake inserted was the basic facility used in the present study. Plexiglass on the dam side of the basin allowed the visualization of the flow situations. This hydraulic distorted model has horizontal and vertical scale ratios of approximately 1 to 360 and 1 to 34, respectively. This gives what appears to be a reasonable balance between compactness, vertical distortion, and feasible Reynolds number. The volume of the lake is an important parameter in determining the destratification time. A portion of the total volume of the Ham's lake is included in a number of tortuous limbs. As a compromise, the limbs were modeled accurately as to depth, width, etc., but bent around so as to keep the overall dimensions down. The destratification device used is a model of the one used by Steichen (10) (see Figure 2).

Model Pump

The pumping device for the model was designed from the prototype pumping device on Ham's lake (see Figure 2) and run by a DC motor. The pump was inserted in the basin and was located at the same nondimensional horizontal and vertical coordinates as in the prototype destratification experiment. Two three-bladed propellers of different sizes were used in four different configurations. Propeller No. 1, cut from .32 cm plexiglass was 3.175 cm in diameter. The blades were twisted to make an angle of approximately 30 degrees with the plane of the propeller hub. Propeller No. 2 was approximately 2.5 cm in diameter. As a first configuration the physical situation in the protytype destratification experiment was modeled. Propeller No. 1 was placed in a simple shroud suspended from the platform where the motor was mounted. Stator vanes were placed on top of the shroud to decrease the rotation of the fluid. In a second configuration a conical skirt was suspended beneath the shroud. The conical skirt which acted as a diffuser was modeled from the skirt used in the prototype discussed by Steichen (10). The skirt was made out of cellulose acetate and connected to the shroud by siliconrubber sealer. The edges were carefully smoothed to prevent any turbulence caused by roughness. The third configuration was a situation where the propeller No. 1 was operated as a free propeller as the shroud and the skirt were removed. The fourth configuration was propeller No. 2 (2.5 cm in diameter) mounted as a free propeller.

Shaft Speed Measurements

Rotational speed measurements were made by means of a magnetic coil and a Beckman electronic counter. The magnetic coil sensed the magnetic

field produced by a magnet strip mounted on the shaft.

Velocity Measurements

Velocity of the water leaving the propeller in each configuration was measured by photographical tracing of dyed portion of the water. Details of the velocity measurements are discussed in Appendix C.

Power Measurements

The power input to the motor was measured by a Hickok digital voltmeter and a Weston ammeter connected in series with the pump and the power supply. The product of current and voltage determined the amount of consumed power. The efficiency of the motor was calibrated by connecting it to a torque meter sensor and measuring the amount of shaft input power at different shaft rotational speeds. The details of power calibration are disucssed in Appendix D.

Data Collection

One set of data was collected during each run by means of the conductivity probe. Resistivity measurements at different depths in the model lake were made by the conductivity probe. These measurements were converted to densities by using the calibration curve for the conductivity probe of Appendix B. Resistivities and time during which measurements were made were both recorded. The experiment was completed when the density of the top was within 10% of the density of the bottom.

Density Measurements

Density measurements were made using conductivity probe specially constructed from flint glass tubing and very thin platinum wire. Details of density measurements by conductivity probe are given in Appendix B.

Experimental Procedure

The first step at the beginning of each experiment with the model was to establish a density profile similar in shape to the prototype lake experiment. Density stratification was established using sodium chloride to increase the density of water by varying amounts. Density differences established in this manner simulate density differences caused by temperature differences. Depending on the exact procedure followed and the specific gravity used, different initial profiles can be obtained. The appropriate procedure needed to reproduce the desired density profile in the model was found and the resulting density versus depth curve was similar in shape to the Ham's lake curve.

The procedure consisted of filling the lake with fresh water up to a height of 21.0 cm. A solution of 1.014 specific gravity was produced in the overhead tank by dissolving pure table salt in fresh water. This solution was slowly introduced into the model at the rate of 1.9 liters/ min with the garden hose located perpendicularly under the pump and approximately 1.25 cm above the bottom until the height of 23.0 cm was reached. Solutions of 1.023 and 1.030 specific gravities were produced by dissolving more salt in the overhead tank. These solutions were introduced into the lake in the same manner until the heights of 24.8 and 26.3 cm were reached. The model was allowed to settle one or two

hours after reaching the final height of .263 meters, in order to let residual currents damp out.

The conductivity probe was calibrated during the preparation of the lake and an initial density profile was measured. Stratification $\frac{\Delta\rho}{\rho}$, where $\Delta\rho$ is a reference density difference (i.e., the difference in density between the top and the bottom), was measured and the desired velocity was calculated in the following manner. The overall Richardson Number J = $\frac{g(\Delta\rho/\rho)H}{U^2}$ of the experiment was initially specified, in some cases to conform to the value used in Steichen's (10) experiment. The stratification $\frac{\Delta\rho}{\rho}$ was measured; a velocity was then chosen so that the Richardson Number combination would exactly match the chosen value for the experiment. The pump was started and the velocity was brought up to its proper value. The timer was started and profiles were recorded at selected time intervals.

Data Reduction

A computer program written by Gibson (16) was modified to perform the necessary calculation needed to plot the stability index versus time curves. The model depth was divided into ten layers. Since the total depth was .263 meters, the model was subdivided into nine divisions of 2.54 cm and one division of 3.43 cm deep. Density measurements were made at the center of each division resembling the closest approximation to the density of that particular layer. The progress of the stability index with time was plotted for each experiment. From these plots nondimensional destratification time, which is an important parameter in proving the validity of modeling technique, was obtained.

CHAPTER V

EXPERIMENTAL RESULTS

A discussion of the results obtained from various experiments on the model of the prototype pump (Shrouded Propeller No. 1) and several modified configurations are presented in this chapter. Results obtained from each configuration are discussed in separate sections. A comparison of the results was made to determine the optimum configuration.

Shrouded Propeller No. 1

Several destratification experiments with different Richardson numbers and velocity conditions were conducted using the No. 1 propeller in a simple shroud. The output data from these experiments were collected by conductivity probes and were analyzed by determining the progression of the stability index with time. Typical density profiles recorded throughout the model destratifier experiments are shown in Figure 6. A total of seven experiments with different Richardson numbers and velocity conditions were conducted. In the most significant experiments the pump output velocity and stratification were adjusted so that the overall Richardson number $J = \frac{g\Delta\rho H}{\rho U^2}$ equaled 0.398 to match the prototype experiment (10). Considering the Richardson number matching of the model and the prototype, $\frac{\Delta\rho}{\rho}$ and U are the only parameters that can be varied to keep the Richardson number at a constant value. Stratification $\frac{\Delta\rho}{\rho}$ was fixed by duplicating the initial condition from

the prototype. The value of the model velocity U was adjusted and fixed to match the Richardson number of the prototype data. Progression of the stability index with nondimensional time was plotted for the model from the measurements. Figure 7 shows this plot with the prototype experiment data superimposed on it. A fourth order polynomial least squared regression curve was fitted for both sets of data. Using the 10% stability index criterion, a nondimensional destratification time of $t_d^* = 0.88$ was obtained for the model experiment. This result is within 15% of the destratification time $t_d^* = .77$ for the prototype. The agreement was actually more successful than expected since the ratio of characteristic times of the prototype to the model was over 2000 and the Reynolds numbers ratio by a factor of 62.

Due to the high velocity operation of the pump during the destratification process for this experiment, the model lake was destratified quickly and time resolution was not as good as some other experiments conducted with different Richardson number conditions. As mentioned earlier in Richardson number matching process, the variation of one of the parameters $\frac{\Delta\rho}{\rho}$ or U causes variation of the other. A series of four experiments were conducted matching the prototype Richardson number. Different stratification conditions were produced for each of these experiments so that four different pump output velocities were used. The results obtained from these experiments are plotted in Figure 8.

Table II lists the important properties of these four experiments which matched the prototype Richardson number. It is generally believed that in the turbulent flow regime most commonly found in lake flows, the characteristics of the fluid motion are not strongly dependent on Reynolds number, provided the Reynolds number of the model is large

enough to preserve the turbulent flow. An attempt was made to analyze this problem in some detail. The four experiments conducted had varying range of Reynolds numbers. The variation of the Reynolds number in each case was made possible by adjusting the destratification and velocity conditions to the values listed in Table II.

Figure 8 shows the progress of stability index with time for these experiments. Comparison of the nondimensional destratification times obtained from this figure (listed in Table II) indicates that at moderately high model Reynolds number, where the model and the prototype Reynolds numbers differ by approximately an order of magnitude, close agreement between the model and the prototype results exists. However, at lower Reynolds numbers deviation from this agreement was indicated. Results obtained from experiments listed under A-5 and A-7 of Table II, where two experiments were conducted at almost identical Reynolds numbers, indicated the repeatability and dependability of the experiments. Results listed in Table II indicate that better mixing is a result of higher rate of the pump operation. Considering the Reynolds number effect on the validity of the modeling technique, it is apparent that increasing the model Reynolds number and bringing it closer to the prototype Reynolds number results in better modeling and closer agreement between the model and the prototype. Since the Reynolds number of the model was smaller than that of the prototype, there is probably some decrease in turbulent mixing, and the model does not replicate the destratification phenomenon. This deviation is lessened by increasing the pump output velocity and therefore increasing the model Reynolds number.

Important properties of all the experiments conducted with No. 1 propeller in a shroud are listed in Table III (experiments A-1 through

A-7) along with the experiments from the other configurations. Values of t_d^* obtained from these experiments for different Richardson numbers were recorded. Plot of Richardson number versus nondimensional destratification time was made in Figure 9.

Another interesting fact is revealed by comparing the density profiles which were measured in the model and the prototype during the destratification process, Figures 4 and 6. Most model density profiles taken during destratification had a stairstep shape characteristic of the lens of intermediate density moving through the lake. The stairstep shape of the density profiles is not as readily apparent in the prototype lake. There are probably several reasons that explain this phenomenon. First, since the Reynolds number of the model is much smaller than the prototype, there is probably some decrease in the turbulent mixing of the lens flow. There are also complicated climatological effects such as sun radiation, surface evaporation and heat transfer, surface wave induced mixing caused by wind or rainfall that increase the amount of mixing and diffusion of the mass and energy in the lake. It is expected that the model under study can replicate only the most important mixing phenomenon, namely the convection set up by the mechanical pump.

Shrouded Propeller With Skirt

Assembling a conical skirt beneath the shroud resulted in the second configuration. The conical skirt was 14.5 cm long and had a base diameter of 6.35 cm. Only one destratification experiment, where the model Richardson number was matched to its prototype value, was conducted in this case. Properties of this experiment are listed in Table III under experiment A-8. Progression of the stability index with time for this

experiment and a similar condition from the simple shrouded case are plotted in Figure 10. Nondimensional destratification times of 1.74 and 1.53 are obtained for conical skirt and shrouded case, respectively. Comparing these two results, it is apparent that operation of a pump with an installed diffuser will result in a longer period of mixing than a pump with simple shroud. However, less power input to the motor was required to drive the system when the skirt was installed. Comparing the destratification efficiencies from Table III, values of .026% and .022% were obtained for the conical skirt and simple shrouded case, respectively. This indicates that pumping systems operating with diffusers may have higher efficiencies than those operating with a simple shroud.

Unshrouded Propeller No. 1

The shroud and the conical skirt were removed and the propeller No. 1 was connected to the shaft. An attempt was made to conduct an experiment that matched the prototype Richardson number condition. The results obtained from such an experiment would be helpful in analyzing the Richardson number effect on different configurations. The prototype Richardson number was matched by adjusting the condition to those listed in Table III under experiment B-1. The progression of the stability index versus nondimensional time for this experiment and an experiment from the simple shrouded case, which was conducted at an almost identical Reynolds number, is presented in Figure 11.

From Figure 11 nondimensional destratification time of t_d^* = .465 is obtained for the free propeller case which compares with t_d^* of 1.53 obtained from the shrouded case. Since both of these experiments were
conducted at an identical Richardson number condition, it is apparent that operation of a pump without a shroud results in a much faster mixing time. In order to gain some insight and prove the validity of this phenomenon, the following experiment was conducted. A destratification experiment with a highly stable stratification condition (high Richardson number) from the shrouded configuration was chosen. The Richardson number and the stratification conditions were matched by adjusting the pump velocity. The progress of the stability index with time was plotted for both cases, Figure 12. A highly stable stratification condition was chosen to increase the mixing time scale compared to the measurements time so that reasonable resolution time was obtained. Nondimensional destratification times of 2.245 and 4.76 were obtained for unshrouded and shrouded cases, respectively. These results are in agreement with the ones discussed earlier in this section.

Considering the power requirements for driving a pumping system, it was apparent that less power was consumed in driving a shrouded propeller than an unshrouded one. An attempt was made to run an experiment where the power input to the shaft for both the shrouded and unshrouded configuration was equal. An experiment from the shrouded configuration with the Richardson number matching the prototype was chosen. From the power input versus rotational speed calibration curve (Figure 13), the power input during this experiment was found to be 3.30 watts. After duplicating the same stratification conditions, a trial and error technique was required to find out the power input to the motor and its corresponding shaft rotational speed which will yield a shaft input power of 3.3 watts. This was simply done by inspection from Figure 13 and referring to Figure 14 (plot of power input to the motor versus

shaft rotational speed). The velocity and the Richardson number were adjusted to the values listed in Table III under experiment B-3 to yield a shaft input power of 3.3 watts. After conducting this experiment, the progress of stability index versus time for both cases were plotted (Figure 15). Destratification times of 15.44 and 12.4 minutes were obtained for the unshrouded and shrouded cases, respectively.

This indicates that operation of a pump with a shrouded propeller will destratify a reservoir quicker than an unshrouded one for the same power consumption rate. Destratification efficiencies of .081% and .069% obtained for shrouded and unshrouded propellers, respectively, indicated the higher efficiency of the shrouded propeller.

Unshrouded Propeller No. 2

Propeller No. 1 was removed and replaced by Propeller No. 2. To analyze the Richardson number effect on different propeller sizes, a stratification and Richardson number conditions from configuration No. 3 were duplicated. (Figure 16 shows the visualization of the lensing phenomenon for this experiment.) Theoretically from the definition of the overall Richardson number $J = \frac{g\Delta\rho H}{\rho U^2}$, velocities of the same magnitude should be expected for both cases. However, as discussed earlier, the exact duplication of stratification conditions are difficult to generate. This introduces a small increase in the velocity (.222 meters/sec compared to .219 meters/sec). The progression of stability index with nondimensional time for this experiment and the experiment from configuration No. 3 case are plotted and shown in Figure 17. Nondimensional destratification times of 2.24 and 5.8 are obtained for No. 1 and No. 2 propellers, respectively. Destratification efficiency of .0034 was obtained for propeller No. 2. Comparison of this value with

destratification efficiency of .026 obtained for unshrouded propeller No. 1 indicates that operation of a pump with the unshrouded propeller No. 1 results in a higher destratification efficiency than unshrouded propeller No. 2, where both pumps operate under the same initial and Richardson number conditions.

Since propeller No. 2 required less power input to drive the system at the same rotational speed as propeller No. 1, an attempt was made to run an experiment with identical power requirements. Trial and error technique and Figures 13 and 14 were used. Conditions were adjusted to those listed in Table III under experiment C-1. The progression of stability index versus time for both propellers consuming the same power was plotted in Figure 18. Destratification times obtained (15.44 and 322 minutes for propellers 1 and 2, respectively) proved that faster mixing time will be obtained when larger propeller is used. Comparison of the destratification efficiencies obtained for both cases also proves the fact that operation of a pump with an unshrouded larger propeller is more efficient than the same system with a smaller propeller, provided both pumps consume the same power to drive the system.

Comparison of the Results

Comparison of the results obtained from different configurations indicates the following: destratification experiments conducted with the shrouded propeller with a skirt resulted in a longer period of destratification time than the simple shrouded case. Operating under the same initial and Richardson number conditions, free propeller No. 1 resulted in a much faster destratification time than propeller No. 1 with a simple shroud. Furthermore, the shrouded propeller had a lower

destratification time t_d and higher destratification efficiency DE than unshrouded propeller No. 1 when operating at the same input power.

Considering the effect of propeller size in destratification phenomenon, free propeller No. 1, operating under the same initial and Richardson number conditions as propeller No. 2, resulted in a much faster destratification time and had a much higher destratification efficiency. This was also true when both propellers operated under a condition of equal power consumption rate.

CHAPTER VI

CONCLUSIONS

The conclusions from this experimental investigation may be listed as follows:

1. Accurate prediction of the prototype destratification experiments can be achieved by means of vertically exaggerated models, using the vertical scale for modeling the destratification device.

2. The appropriate nondimensional parameters are the overall Richardson number $J = \frac{g\Delta\rho H}{U^2}$, and a characteristic time obtained from the volume of the lake divided by the volume discharge rate of the pump.

3. Operation of a pump with a shrouded propeller will result in a higher destratification efficiency than a pump with an unshrouded propeller, when both pumps have the same power consumption rate.

4. The efficiency of a pumping system operating with larger unshrouded propeller is higher than a pumping system operating with a smaller unshrouded propeller and consuming the same amount of power.

A SELECTED BIBLIOGRAPHY

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- (1) Harleman, D. R. F. and P. J. Ryan. "Temperature Prediction in Stratified Water." M.I.T. Civil Engineering Department Technical Report No. 16130 DJH. Cambridge, Mass.: U. S. Environmental Protection Agency, April, 1971.
- (2) Symons, J. M., W. H. Irwin, and G. G. Robeck. "Important Water Quality Changes Caused by Mixing." <u>J. San. Eng. Div., ASCE</u>, Vol. 96, No. SA2 (April, 1967), pp. 1-13.
- (3) Symons, J. M., W. H. Irwin, E. L. Robison, and G. G. Robeck. "Impoundment Destratification for Raw Water Quality Control Using Either Mechanical or Diffused-Air-Pumping." J. Amer. <u>Water Works Assoc</u>., Vol. 59, No. 10 (October, 1967), pp. 1268-1291.
- (4) Knoppert, P. L., J. J. Rook, T. J. Hofker, and G. Oskam. "Destratification Experiments at Rotterdam." J. Amer. Water Works Assoc., Vol. 62, Pt. 2 (1970), pp. 448-454.
- (5) Symons, J. M., W. H. Irwin, R. M. Clark, and G. G. Robeck. "Management and Measurement of DO in Impoundments." <u>J. San.</u> <u>Eng. Div., ASCE</u>, Vol. 96, No. SA6 (December, 1967), pp. 181-200.
- (6) Lackey, R. T. "A Technique for Eliminating Thermal Stratification in Lakes." J. Amer. Water Resources Assoc., Vol. 8, No. 1 (February, 1972), pp. 46-49.
- (7) Hogan, W. T., F. E. Reed, and A. W. Starbird. "Optimum Mechanical Aeration Systems for Rivers and Ponds." Report No. 16080 D00. Littleton, Mass.: Littleton Research and Engineering Corp., November, 1970.
- (8) Irwin, W. H., J. M. Symons, and G. G. Robeck. "Impoundment Destratification by Mechanical Pumping." <u>J. San. Eng. Div.</u>, <u>ASCE</u>, Vol. 92, No. SA6 (December, 1966), pp. 21-40.
- (9) Quintero, J. E. and J. E. Garton. "A Low Energy Lake Destratifier." Paper No. 72-599. Chicago, Ill.: American Soc. of Agr. Eng., December, 1972.
- (10) Steichen, J. M. "The Effect of Lake Destratification on Water Quality Parameters." (Ph.D. thesis, Oklahoma State University, July, 1976.)

- (11) Dake, J. M. and D. R. F. Harleman. "Thermal Stratification in Lakes: Analytical and Laboratory Studies." J. Amer. Water Works Assoc., Vol. 5, No. 2 (April, 1969), pp. 484-495.
- (12) Ligget, J. A. and K. K. Lee. "Properties of Circulation in Stratified Lakes." J. Hydraulics Div., ASCE, Vol. 97, No. H41 (January, 1971), pp. 15-29.
- (13) Ditmans, J. D. "Mixing of Density Stratified Impoundments with Buoyant Jets." W. M. Keck Lab. of Hydraulics and Water Resources, Report No. KH-R-22. Pasadena, Calif.: California Institute of Technology, September, 1970.
- Boericke, R. R. and D. W. Hall. "Hydraulics and Thermal Dispersion in an Irregular Estuary." <u>J. Hydraulics Div., ASCE</u>, Vol. 100, No. H41 (January, 1974), pp. 85-102.
- (15) Odell, G. M. and S. G. Kovasquay. "A New Type of Water Channel with Density Stratification." <u>J. Fluid Mechanics</u>, Vol. 50, Pt. 3 (March, 1971), pp. 535-543.
- (16) Gibson, T. A. "Investigation of Artificial Lake Destratification --A Hydraulic Model Study." (M. S. thesis, Oklahoma State University, July, 1974.)
- (17) Fischer, M. B. and E. R. Holley. "Analysis of the Use of Distorted Hydraulic Models for Dispersion Studies." <u>Water Resources</u> Research, Vol. 7, No. 1 (February, 1971), pp. 46-51.
- (18) Francis, J. R. D. "Scaling of River and Estuary Models." <u>The</u> Engineer (London), Vol. 190 (September, 1960), pp. 329-331.
- (19) Shian, J. C. and R. R. Rumer. "Adjustment of Friction in Hydraulic Models of Lakes." <u>J. Hydraulics Div., ASCE</u>, Vol. 99, No. H412 (December, 1973), pp. 2251-2262.
- (20) Barr, D. I. H. "Model Simulation of Vertical Mixing in Stratified Flowing Water." <u>The Engineer</u> (London), Vol. 215 (January, 1963), pp. 345-352.
- (21) Keulegan, G. H. "The Mechanism of an Arrested Saline Wedge." <u>Estuary and Coastline Hydrodynamics</u>. New York: McGraw-Hill Book Co., 1966, pp. 56-75.
- (22) Barr, D. I. H. and A. M. M. Hassan. "Densimetric Exchange Flow in Rectangular Channels." <u>La Houille Blanche</u>, Vol. 18, No. 7 (November, 1963), pp. 757-766.
- (23) Toetz, D., J. Wilhm, and R. Summerfelt. "Biological Effects of Artificial Destratification and Aeration in Lakes and Reservoirs--Analysis and Bibliography." Bureau of Reclamation Report REC-ERC-72-33. Denver, Colo.: U. S. Department of Interior, 1972.

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TABLES AND FIGURES

TABLE I

Parameters	Prototype Experiment	Model Experiment A-4	Units meters ³	
Lake volume V	1.15 x 10 ⁶	. 348		
Maximum depth H	9.0	.263	meters	
Stratification, $\frac{\Delta \rho}{\rho}$.0025	.026		
Shroud diameter	107	3.76	centimeters	
Pump flow rate, Q	0.67	4.5×10^{-4}	meters ³ /sec	
Average pump outlet velo- city, U	0.74	0.41	meters/sec	
Richardson number, J	0.40	0.40		
Characteristic time, t _c	1.72 x 10 ⁶	767	sec	
Reynolds number, Re = UH	6.56 x 10 ⁶	1.06 x 10 ⁵		

PARAMETERS OF PROTOTYPE AND MODEL LAKES FOR DESTRATIFICATION EXPERIMENTS

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TABLE II

Experiment	$(\text{Re})_{\text{m}} = \frac{\text{UH}}{v}$	$(\text{Re})_{\rho} = \frac{\text{UH}}{v}$	$J = \frac{g(\Delta \rho / \rho)H}{U^2}$	<u>Δρ</u> ρ	U(Meters/ sec)	t [*] d	
A-4	1.057 x 10 ⁵	6.56 x 10 ⁶	.398	.0026	.409	.88	
A-5	6.312×10^4	6.56 x 10 ⁶	. 398	.0092	.244	1.53	
A-6	8.565 x 10 ⁴	6.56 x 10 ⁶	. 398	.0169	. 331	.95	
A-7	6.382 x 10 ⁴	6.56×10^{6}	. 398	.0094	.247	1.48	

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PROPERTIES OF MODEL EXPERIMENTS MATCHING THE PROTOTYPE RICHARDSON NUMBER

TABLE III

PROPERTIES OF MODEL DESTRATIFICATION EXPERIMENTS FOR DIFFERENT CONFIGURATIONS

Experiment	$J = \frac{g(\Delta \rho / \rho)H}{U^2}$	U(Meters/ sec)	t _d (min)	∆(P.E.) KW-HR	Motor Input Power (Watts)	Shaft Input Power (Watts)	D.E. %
A-1	.643	. 308	49.5	5.7 x 10 ⁻⁷	8.20	2.40	.029
A-2	2.494	.162	432	5.74 x 10 ⁻⁷	5.98	.85	.0094
A-3	1.408	.232	108.3	7.1 $\times 10^{-7}$	7.20	1.75	.022
A-4	.398	.409	12.4	5.5 x 10^{-7}	9.20	3.30	.081
A-5	. 398	.244	32.75	2.2 x 10^{-7}	7.35	1.94	.020
A-6	.398	.331	15	3.8×10^{-7}	8.40	2.65	.057
A-7	. 398	.247	31.33	2.24 x 10^{-7}	7.40	1.98	.022
A-8*	. 398	.253	35.95	2.3 x 10^{-7}	6.264	1.50	.026
B-1	. 398	.265	12.88	2.5×10^{-7}	8.00	2.30	.050
B-2	1.408	.219	75	5.9 x 10^{-7}	7.30	1.80	.026
B-3	.602	.314	15.44	5.9 x 10^{-7}	9.11	3.30	.069
C-1	1.40	.222	322	6.0 x 10 ⁻⁷	9.20	3.30	.0034

A - Shrouded propeller No. 1.

B - Unshrouded propeller No. 1.

C - Unshrouded propeller No. 2.

*Shrouded with skirt.



Figure 1. Schematic of Ham's Lake



Figure 2. Schematic of the Mechanical Pump Used by Garton





Figure 4. Density Profiles Recorded Throughout the Prototype Destratifier Experiment







Figure 6. Density Profiles Recorded Throughout the Model Destratification Experiment A.4



Figure 7. Comparison of Stability Index Measurements Made in the Model With Those Made in the Prototype Lake During Destratification





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Figure 10. Progression of the Stability Index With Time for Shrouded and Skirted Propeller



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Figure 11. Progression of Stability Index With Time for Shrouded and Unshrouded Propeller No. 1 (Richardson Number .398)









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Elapsed time 5 seconds

Elapsed time 30 seconds



Elapsed time 10 seconds



Elapsed time 50 seconds





Elapsed time 20 seconds

Elapsed time 300 seconds

Figure 16. Visualization of the Lensing Phenomenon for Free Propeller No. 2









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Figure 19. Schematic Diagram of Conductivity Probe



Figure 20. Sample Calibration Curve for a Conductivity Probe



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CONDUCTIVITY PROBE

APPENDIX B

The method of constructing the conductivity probe proceeds as follows:

First, a 3 mm outside diameter flint glass tube was heated. When the proper temperature was reached, the glass tube was drawn down to an approximate inside diameter of .07 mm. Then a platinum wire of approximately 28 μ m in diameter was threaded into the glass tube. The smaller end of this tube was reheated, sealing the platinum wire inside. The tip was carefully shaped with fine sandpaper. The electrolytic solution was made by dissolving 0.3 gram of chloroplatinic acid $(H_2Ptc1,6H_2O)$, and .003 gram of lead acetate $(Pb_{20}(CH_3COO)_2)$ in 10 ml of water. The tip was placed in this solution and standard plating technique was used, and the tip was coated with platinum black. A 5 mm o.d. flint glass tube epoxied to the 3 mm o.d. glass tube provided the main body of the probe. Figure 19 shows the schematic diagram of the probe with the electrical network. The probe tip and a wire mesh screen were used as two electrodes. Immersing these two in the salt water solution completed the circuit of an A-C impedance bridge. Type 1650A impedance bridge was utilized to measure the resistivity of the solution at the probe tip. The resistivity measurements were converted to densities through the calibration curve for the conductivity probe. The conductivity probe was calibrated by measuring the resistivity of several salt solutions over a range of known density. This calibration chart was plotted and is shown in Figure 20. In order to measure a particular density profile in the model, the resistivities were recorded at several different depths. These values were converted to density readings from the calibration curve of density versus resistivity. Then the plot of density versus depth was plotted.

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VELOCITY MEASUREMENTS

APPENDIX C

The velocity of the water leaving the propeller was calibrated using a dye tracing technique. A 16 mm Pailard-Bolex high speed movie camera was placed on the side of the model by the dam. Thin strips of black tape were placed on the plexiglass sidewall to serve as markers. The motor was started and the shaft RPM was adjusted to the desired value. The camera was started and the blue dye was injected through a ring-type dye injector placed above the propeller. The dye injector was made out of .32 cm o.d. hypodermic tube. Eight small holes (.5 mm in diameter) were drilled on the ring portion of the injector at approximately the same distances apart and one end of the injector was sealed with the epoxy. The free end of the hypodermic tube was fitted in a tygon tubing and sealed by silicon rubber. The tygon tubing was connected to a dye pot located on the side of the model.

Opening a small value allowed the dye to enter the water. The movement of the dye leaving the propeller was recorded on film. The shaft RPM was then incremented to a higher value and the same procedure was followed. Several different shaft RPM's were recorded. Data reduction from these recorded films consisted of measuring the distance that the dye front traveled in the duration of five frames. The time during which the dye front traveled this distance was known from the speed setting on the camera. The velocities were calculated by dividing the distance traveled to the time elapsed. The results of this calibration as a function of rotational speed is shown in Figure 21.
РОМЕВ МЕАSUREMENTS

APPENDIX D

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Power input to the motor was measured by means of a Hickok digital voltmeter and a Weston ammeter. The product of the voltage and current determined the amount of power input to the motor. The plot of motor input power versus shaft rotational speed for different configurations is shown in Figure 14. The plotted data indicates that the shrouded propeller requires less power input to the motor to drive the system at the same speed as the unshrouded propeller. This phenomenon is more apparent at the higher propeller speeds. However, the efficiency of the motor was changed by varying the propeller speed. An attempt was made to measure the motor efficiencies at different shaft rotational speeds. In order to accomplish this purpose the motor was connected to a 22.6 Newton-meters Lebow torque meter sensor with the electric brakes. A calibrated tachometer was connected to the motor shaft to measure the shaft rotation. The motor was started and the amount of torque produced for different shaft rotational speeds were recorded. The measured torque values were converted to power quantities through the relation

Torque = power into the shaft x RPM.

Figure 22 is a plot of measured torques for different values of rotational speed and constant power inputs to the motor. Obtained from this plot is a plot of shaft input power versus shaft rotational speed corresponding to different motor input powers (see Figure 13).

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СОМРИТЕК РКОGRAM

APPENDIX E

0: 1→X

4:

5:

8:

9:

10:

13:

6: 0→X

151→X

12: 150→X

14: 151→X

15: RX→Y

19: 0→R31

23: 101→X

26: 100→X

25:

11: SPC 5;PRT "VOLUMES"

17: PRT "TOTAL VOLUME"

20: SPC 2;ENT "TIME",C]

21: SPC 3;PRT "TIME=",C1

22: ENT "RESP DENS=R101", R101

SPC 5; PRT "DENSITIES"

24: X+1-X;ENT "NEXT DENS",RX;IF RO>X-100;GTO +0

18: SPC 2; PRT Y

- ENT "NO OF Y DIV?", RO 1:
- 2: PRT "THE NO OF"; PRT "DIVISIONS IS", RO

- 3: ENT "DIV CENT HIGH=R1",R1

X+1→X;ENT "NEXT HIGHT",RX:IF RO>X;GTO +0

X+1→X;ENT "NEXT VOLUME",RX;IF RO>X-150;GTO +0

SPC 5;PRT "HIGHTS OF DIV":PRT "CENTERS ABOVE": PRT "BOTTOM"

7: X+1→X;PRT RX: IF RO>X;GTO +0

ENT "RESP VOLUM=R151",R151

X+1+X;PRT RX;IF R0>X-150;GT0 +0

16: X+1→X;RX+Y→Y;IF RO>X-150;FTO +0

- 27: X+1+X;PRT RX;IF R0>X-100;GT0 +0
- 28: 100→X
- 29: $X+1 \rightarrow X$; RX*R(X+50) \rightarrow R(X-50); IF RO>X-100; GTO +0
- 30: SPC 5;PRT "WEIGHT OF";PRT "RESPECTIVE";PRT "DIVISIONS"
- 31: 50→X
- 32: X+1-X;PRT RX;IF RO>X-50;FTO +0
- 33: 51→X
- 34: RX→B
- 35: X+1→X;RX+B B; IF RO>X-50;GTO +0
- 36: IF R31>0;B→R41
- 37: R31+1→R31
- **38:** 1→X
- 39: RX*R(X+50)→A
- 40: X+1+X;RX*R(X+50)+A→A; IF RO>X;GTO +0
- 41: A/B→C;SPC 5
- 42: PRT "THE CENTER OF"; PRT "GRAVITY IS", C; PRT "FT ABOVE BOTTOM"
- 43: B/Y→R201;SPC 2
- 44: PRT "AVERAGE DENS",R201
- 45: C*R41→R202
- 46: SPC 5;PRT "P.E. OF";PRT "THE LAKE IS",R202
- 47: R202*5.05E-7→R203
- 48: SPC 1;PRT "OR";SPC 1;PRT R203;PRT "HP-HRS"

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- 49: SPC 5;GTO 20
- 50: STP
- 51: END

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Computer Nomenclature

- A: Sum of all the first moments of areas
- B: Sum of all the weights of the divisions
- C: Center of gravity of the lake above the bottom
- Cl: Time at which density profile is recorded
- Y: Total volume of the divisions
- RO: No. of Y divisions
- R1→R10: Center of divisions above bottom
 - R31: Logic control variable
 - R41: Logic control variable
- R51→R60: Weight of the respective divisions
- R101+R110: Respective densities of the divisions
- R151→R160: Volumes of the divisions
 - R201: Average density
 - R202: Potential energy of the lake in ft-lbf
 - R203: Potential energy of the lake in HP-HRS

Computer Flow Chart





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SCALING PROCEDURE

APPENDIX F

BACKGROUND

The classical scaling procedure in hydraulic modeling proceeds as follows: 1.) A geometrical scaling ratio is established between model and prototype. For example, if this is 1:30, some characteristic length of the hydraulic model is one thirtieth as large as that same length of the prototype lake. 2.) All quantities are normalized by dividing them with a reference quantity from the prototype, resp. from the model. For example, all lengths are divided by the characteristic length chosen; these normalized lengths are then identical in model and prototype, if the model is scaled correctly, since the corresponding non-normalized lengths in model and prototype are all supposed to be in the chosen scaling ratio.

3.) Similarly, the velocity at any point is normalized by dividing it by a reference velocity arising out of the boundary conditions, such as the characteristic velocity of some inflow; the pressure is normalized by dividing it by the stagnation pressure corresponding to the reference velocity, etc. If the modeling is successful, all these normalized variables will be identical between model and prototype.

4.) Then, the governing equations -- in the case of Newtonian fluid flow, the Navier-Stokes equations -- are written out. The dimensionless coefficients of the differential terms define the equation and determine the solution; if these dimensionless coefficients are the same in model and prototype equation, and if the normalized boundary conditions are the same, there will be strict similitude between model and prototype, and the observed normalized variables will be identical between them.

5.) Some of these dimensionless coefficients are the Mach number $\frac{\cup}{a}$ and the inverse of the Reynolds number

$$Re = \frac{UD\rho}{u} = \frac{UD}{v}$$

where U is the reference velocity and D is the characteristic length, etc.^{*} As a rule, it is impossible to construct a model in which all dimensionless numbers match the prototype; hence, it is necessary to decide which are important. For example, if the Mach number is much smaller than one, certain terms in the governing equations are unimportant to the result, and matching the Mach number between model and prototype may be neglected -- this is true of lake models. Similarly, if the inverse of the Reynolds number is very small, the Reynolds number may by unimportant -- this is not necessarily true in lake models, and the Reynolds number must generally be considered. However, the accuracy of the modeling may not be extremely sensitive to the exact matching of Reynolds number between model and prototype.

6.) If the fluid used in the model has the same kinematic viscosity v as the prototype, reducing the characteristic length in the model requires raising the characteristic velocity in the same ratio. Hence velocities in the model are higher than in the prototype. This has its limits -- for example, if this leads to a large Mach number. In a lake model, the limit is more likely to be in the Froude number, another dimensionless coefficient. 7.) The Froude number, for example in the form

$$Fr = \frac{U^2}{gD}$$

is part of the governing equation if there is a free surface, as on a lake, with a high density below it and a negligible density above it. When we are investigating slow currents in lakes, we neglect it, since the surface effects are negligible and do not influence the flows. However, in the model the Froude number is larger; it may, for example, reach a critical value at an inflow, so that there is a standing wave called a "hydraulic jump"; or the surface depression over pump inlet may be so great that air is entrained. It is necessary to limit the velocity increase and size reduction in the model to make sure that the Froude number does not become important.

8.) The consequence of limiting Froude number is that either the models must be large (i. e. the characteristic length reduced by only a moderate ratio, and the reference velocity increased by only the same ratio); or that the Reynolds number is lower in the model than in the prototype (i. e. the reference velocity is not increased in proportion to the scaling ratio). 9.) There is considerable experience in the use of too-small Reynolds numbers in models. It is known that this deviation from strict similitude leads to only moderate errors, if the flow regimes (i. e. laminar or turbulent flow) are still the same in the model. We will later discuss some instances where there is less mixing in the model, due to the lower Reynolds number. 10.) Another possible compromise is the use of geometric distortion. For example, the horizontal scale may be 1:300, so that the model will fit into a given facility; while the vertical scale is only 1:30, so that lower Froude numbers and higher Reynolds numbers (for the boundary layer on the bottom) are possible. However, this represents a deviation from the prototype which cannot be analyzed in terms of similitude; we found it necessary to verify this procedure experimentally, as we will outline later.

11.) If there are density stratification in the model, another dimensionless coefficient appears in the governing equation, in the form of a densimetric Froude number or its inverse, a Richardson number

$$Ri = \frac{g \triangle \rho D}{\rho U^2}$$

where $\Delta \rho$ is a reference density difference and D is the characteristic length, taken vertically if there is geometric distortion. To match Richardson number between model and prototype, where the depth of the model is smaller but its reference velocity greater than in the prototype, the density difference in the model must be greater in order to achieve the same Richardson number. This is discussed in more detail below, since the Richardson number relates to the terms of the governing equation which are most important to the phenomena with which we are concerned here.

EXPERIMENTAL PROCEDURES & CONCLUSIONS

As pointed out in Paragraph 11. above, a hydraulic model of a stratified lake requires a greater density variation than the prototype, if the Richardson number is to be matched, and the Reynolds number maintained in the same general range or regime in both model and prototype. The density differences in the prototype lake may be due to temperature differences; in the model, thermal stratification is impractical -- the required temperature differences are too great, the boundary conditions of conduction from the bottom of the lake or radiation, convection, and mass transfer from the surface are not the same in the model and the prototype, etc. However, if the fluid has similar thermal and molecular diffusivity (i.e. if the Lewis number is near 1 or if the major mechanism of mixing is turbulence rather than diffusion -- both of which conditions are true in our case -- density differences due to temperature may be modeled by density differences due to dissolved salts.

There are a number of salts which can increase the density of water by about 80%; common table salt can theoretically give about a 20% increase -- much less if the solution has to be clear -- and is convenient and inexpensive, since a few percent weight density increase turned out to be adequate for our studies.

Stratified conditions were obtained by filling the basin slowly from the bottom with increasingly dense salt solutions.

The stratification was measured at various depths with a conductivity probe; from the conductivity and the calibration curves we had developed, we obtain the local salt content and density.

In order to verify the effect of vertical distortion, as discussed in Paragraph 10. above, we first constructed two simple basins that were identical, except that one was twice as deep as the other. They were long and narrow, with transparent sides; each one had the identical inlet, modeled after the inlet into a real lake, but scaled to the depth of each model (Figure 1).

A large number of tests was run with these models; they consisted of establishing a strongly stratified initial condition, and the observation of the inflow and dispersion of a dyed liquid of intermediate density. The observations included sketches of the pattern of dispersion, photographic determination of the speed with which the dye front advanced, and recording of the density profile before and after the inflow $[1,2]^*$.

The conclusions included the following:

(a.) Exact matching of the Richardson number is crucial to the experiment;

^{*}numbers in brackets refer to references listed at the end of the paper

(b.) Reasonable matching of the density profile's shape is important; (c.) Some difficulties were encountered due to the geometrical distortion when the flow passed along a bottom surface which opened up or descended much more abruptly in the deeper model than in the shallower model; a vertically distorted model may allow a gravity flow to detach from the bottom more quickly;

(d.) Although the vertical distortion did not change gross model behavior,
local oscillations and mixing were sensitive to the distortion and the
errors in matching local Reynolds number in the shear layers;
(e.) The typical behavior of an inflow is to find its correct place in the
density profile and then proceed horizontally in the general direction of
its initial flow, with some sinuous deviation.

After some expertise had been developed in the experimental and modeling technique, a model of a small lake (Ham's lake) was constructed (see Figure 2). The vertical scale of the model is in the order of 1:30, the horizontal about 1:300. This gives us what appears to be a reasonable balance between compactness, vertical distortion, and feasible Reynolds number.

This lake has a number of tortuous limbs, which we wanted to include in the model, without making the model smaller in scale. As a compromise, the limbs were modeled accurately as to depth, width, etc., but bent around so as to keep the overall dimensions down. In this lake, a mechanical destratification device consisting of a propeller pointed downward into the water, was modeled after one which had been in operation in the prototype lake (see Figure 3).

Preliminary experiments showed the following new conclusions [3, 4]: (f.) The mixing took place largely in the vicinity of the destratification propeller;

(g.) the mixed, intermediate density liquid flowed outward at its proper level as a "lens".

As a result, it was decided to scale the propeller about 1:30 like the vertical scale, so that the near-field modeling would be undistorted.

At the same time, for the purpose of obtaining time scales of mixing the overall lake, the volume of the lake divided by the volume flow rate of the propeller was chosen as a characteristic time. This relates the mixing rate to the total basin to be mixed.

Using this approach, tests were conducted for various conditions [3,4], observing the dispersion of dye from above and through the dam, and plotting a stratification index against time. We obtained the following conclusions:

(h.) The time in which the mixed fluid reaches the furthest parts of the

lake is short compared to the time necessary for total mixing. Hence, our approach which concentrates on the mixing process (but distorts the dispersion time) is appropriate for predicting the progress of destratification as an overall process, for our range of parameters.

(i.) Similarly, the density profiles in the model are substantially identical at all stations at any given time, as had also been observed in the lake;
(j.) The Reynolds number was matched well enough to give similar turbulence and mixing rates in the near field, and the model time required for complete destratification corresponded reasonably with the lake;
(k.) The added mixing of the dispersing lens in the far field was less in the model, as discussed in Paragraph 9. above; hence the profiles in the model, though similar to the lake in an overall way, were more abrupt or "stair-step-like" than profiles obtained in the lake during mixing.

The result listed under (j.) permits us to use this hydraulic modeling approach for destratification prediction.

CURRENT WORK

We are currently engaged with comparing different mixing devices in the model. In particular, we are interested in developing a more efficient mixing device. In the past, this has been thought to lie in the direction of devices which turn over large quantities of water at a low velocity. We have obtained the following intermediate result:

(l.) If the downward velocity of a mixing jet is not adequate, when applied to a strongly stratified lake, the lake will not mix all the way to the bottom.

FUTURE WORK

Since the modeling procedure which we have shown to work is not sensitive to the exact shape of the shore line, but only to the correct modeling of the mixing device and to the volume of fluid available at each level of stratification, we hope to show that we can model lakes other than Ham's lake with our model. The lake to be modeled should have a similar ratio of average depth to maximum depth (such as Lake of the Arbuckles), so that the distribution of volume with depth is similar. We will then set our scale of vertical lengths from the ratio of model depth to lake depth, and the horizontal scale from the square root of the ratio of areas. For a large lake, this will lead us to more extreme scales and a poorer match on Reynolds number, the effect of which will require further verification.

REFERENCES

- P. M. Moretti and D. K. McLaughlin, "Distribution and Mixing of Inflow into Stratified Lakes: A Hydraulic Model Study," OWRR A-044-Okla. Annual Report, Oklahoma State University, Stillwater, June, 1973.
- [2] S. J. Vogel, D. K. McLaughlin, and P. M. Moretti, "Hydraulic Model Studies of Distribution and Mixing of Inflow into Stratified Lakes with Vertical Scale Distortion," OWRR A-044-Okla. Research Project Completion Report, Oklahoma State University, Stillwater, June 1973.
- [3] P. M. Moretti and D. K. McLaughlin, "Distribution Phenomena in Stratified Lakes," OWRR A-050-Okla. Annual Report, Oklahoma State University, Stillwater, June 1973.
- [4] P. M. Moretti and D. K. McLaughlin, "Mixing Phenomena in Stratified Lakes," OWRR A-050-Okla. (Phase 1.) Technical Completion Report ER-75-ME-1, School of Mechanical and Aerospace Engineering, Oklahoma State University, Stillwater, July, 1974.



Figure 1. Model Basin for Inlet Flows



Figure 2. Prototype of Lake Model



Figure 3. Prototype of Mechanical Stratification Device

DEFLECTOR TEST

VEPENDIX G

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RESULTS OF EXPERIMENT MARCH 4, 1976 (VERTICAL DEFLECTOR)

In previous experiments, we found that the top layers in the model lake were last to destratify. Of course we wanted to destratify the top layers sooner, so on Thursday, March 4, we decided to investigate the effects of a deflector under the propeller, concave upward. The deflector was an alternative to a submersible pump on the bottom of the lake pumping upward. Hopefully, this would have forced the lower layers to mix with the upper layers sooner.

An illustration of Thursday's set-up is given in Figure 1. The propeller shaft was extended 1.5 inches, setting the propeller at 3.25 inches under the surface. A small aluminum pie plate was attached by means of a wire to the underside of the pump housing, and set at 3.4 inches under the propeller. These dimensions were arbitrary, but they were satisfactory since this was merely a trial run to test the effects of this particular deflector.

The lake was filled and stratified according to the specifications given in Nader Sharabianlou's "Hydraulic Modeling of Mechanical Destratification of Lakes." These are the specifications that are always used. With the lake "settled" and the probe calibrated, we obtained a density profile of the lake before the pump was started. This was t = 0, and the profile, shown in Figure 2a, was as expected. The pump was started and we made certain that all initial conditions and assumptions were met: namely that no surface effects were present. These include cavitation around the shaft at the surface and the injection of air bubbles into the water.

The run was typical. We made density measurements for three 5-minute intervals and then the remainder in 10- to 15-minute intervals. It was obvious from just the resistance readings that the lower and middle layers were mixing more rapidly than in previous runs. But the resistance in the top layer (the first two readings, one at 0 inches and the other at 0.675 inches) remained constant throughout the run. Figure 2b shows the last density profile measured before we decided to end the run.

To see what was happening, dye was injected at the propeller, and we watched its progress through the lake. First it was noted that the deflector did not deflect the flow upward as hoped, but rather it tended to diverge the flow outward horizontally all around, as shown in Figure 3. Also we checked that the dam did not interfere with or contribute significantly to the flow of the dye throughout the lake.

But what was most significant and surprising was that the top layer was virtually untouched! A clear layer of water about 7/8" deep remained on top while the remaining 9.475 inches mixed and became

homogeneous with blue dye as shown in Figure 4. There seemed to be absolutely no mixing between the two layers, and the surface between the two layers was so distinct that it seemed as if two immiscible liquids had been carefully poured into the lake.

With time, the lower layer would probably have pushed up all the way to the surface, but the purpose of the deflector was to reduce the time to destratification. It is possible that the propeller was too deep to pump any of the top layer down, and since the deflector did not deflect upward as hoped, the top layer remained uneffected. We plan to make a run without the deflector but with the propeller at the same depth to test this idea.



Figure 2a

Figure 2b





Figure 4

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Figure 3



LOWERED PROPELLER TEST

V DEENDIX H

Results of Experiment - March 23, 1976

(Propeller at 3.25 inches, without deflector)

On March 4, 1976, the propeller used in destratifying the model lake was lowered to 3.25 inches under the surface. A deflector concave upward was positioned 3.40 inches under the propeller. The configuration is described in the report of March 4. We had hoped that the deflector would divert some of the flow from the propeller up to the surface in order to destratify the top layers sooner. Even though the middle and lower layers were destratified more rapidly than in other configurations, the top layer was virtually untouched. This was evident from the density profiles and the injection of dye into the lake. It was thought that the depth of the propeller reduced its effectiveness in pulling the top layer down, coupled with the observation that the deflector did not deflect upward as well as we had hoped.

On March 23, 1976, we removed the deflector and left the propeller at 3.25 inches under the surface in order to test this idea. An illustration of this configuration is given in Figure 1.

As before, the lake was filled and stratified according to the specifications given in Nadar Sharabianlou's report. Having given the lake one hour to "settle", and having calibrated the resistivity probe, a density profile of the lake was taken to insure stratification. This reading was t=0, and the result is shown in Figure 2. This was a typical profile for t=0, as it should have been.

The motor was started, and the propeller's angular velocity was set at 9.4 r.p.s. (as was before with the deflector). This value is determined by a Richardson's number of 0.398, also given in Nadar Sharafianlou's report. Readings were taken at the end of consecutive 10-minute intervals. As with the deflector, the lower and middle layers were destratified within a half-hour, which is comparatively rapid. But once again the top layer remained static. Figure 3a shows the density profile at t=72005 (two hours). This had been the norm since t=24005.

We decided to let the propeller run for another hour as we met class. At t=12,0005 (3 1/2 hours), Figure 3b shows the same general profile with the density in the subsurface region reduced somewhat. It is possible that this is due to some destratification, but it is more likely the result is difusion.

Figure 4 shows a cross-section of the lake at t=12,0005. We did not inject dye into the lake on this run. But rather the difference in diffraction characteristics between the pure and salt water were clearly visible at a depth of 1.375 inches below the surface. This layer had remained in that position for the entire run since t=24005.

From the results of this and the previous run with the deflector, it is apparent that the failure to destratify the top layer of the lake is due to the depth of the propeller and not due to the deflector. Since a lower propeller destratifies the subsurface layers more rapidly than with other configurations we've tried, we feel that it is worthwhile to test the possibilities of raising the propeller slightly in order to reach the top layer of the lake. We hope to make several runs of this sort in the near future.









Figure 3a

Figure 3b



